

# **General Certificate of Education (A-level) January 2011**

**Mathematics** 

**MD01** 

(Specification 6360)

**Decision 1** 

Mark Scheme

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### **Key to mark scheme abbreviations**

m or dM mark is dependent on one or more M marks and is for method A mark is dependent on M or m marks and is for accuracy B mark is independent of M or m marks and is for method and accuracy E mark is for explanation  √or ft or F follow through from previous incorrect result  CAO correct answer only  CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)  dp decimal place(s)	M	mark is for method
B mark is independent of M or m marks and is for method and accuracy E mark is for explanation  √or ft or F follow through from previous incorrect result  CAO correct answer only CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	m or dM	mark is dependent on one or more M marks and is for method
E mark is for explanation  √or ft or F follow through from previous incorrect result  CAO correct answer only  CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	A	mark is dependent on M or m marks and is for accuracy
CAO correct answer only CSO correct solution only AWFW anything which falls within AWRT anything which rounds to ACF any correct form AG answer given SC special case OE or equivalent A2,1 2 or 1 (or 0) accuracy marks -x EE deduct x marks for each error NMS no method shown PI possibly implied SCA substantially correct approach c candidate sf significant figure(s)	В	mark is independent of M or m marks and is for method and accuracy
CAO correct answer only  CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	E	mark is for explanation
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AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	AWRT	anything which rounds to
SC special case OE or equivalent A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error NMS no method shown PI possibly implied SCA substantially correct approach c candidate sf significant figure(s)	ACF	any correct form
OE or equivalent A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	AG	answer given
A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	SC	special case
-x EEdeduct x marks for each errorNMSno method shownPIpossibly impliedSCAsubstantially correct approachccandidatesfsignificant figure(s)	OE	or equivalent
NMS no method shown PI possibly implied SCA substantially correct approach c candidate sf significant figure(s)	A2,1	2 or 1 (or 0) accuracy marks
PI possibly implied SCA substantially correct approach c candidate sf significant figure(s)	–x EE	deduct x marks for each error
SCA substantially correct approach c candidate sf significant figure(s)	NMS	no method shown
c candidate sf significant figure(s)	PI	possibly implied
sf significant figure(s)	SCA	substantially correct approach
8 8 0	c	candidate
dp decimal place(s)	sf	significant figure(s)
	dp	decimal place(s)

#### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

## **MD01**

MIDUI				
Q	Solution	Marks	Total	Comments
1(a)				
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1		$(6\times6)$ matrix labelled with
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			some $\sqrt{s}$ or $\times s$ or 0's or 1's or $-s$
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			Some v s or x s or o's or r s or - s
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	A1	2	CAO
		711	2	CHO
(b)	A-4+E			
	A-5+B	M1		1 correct
	C-4+E $6-D+2$			
	6-D+2	M1		1 correct, from a different start point
	6-B+5			
	1-F+3			
	4-5+R-3+F-1			
	A-5+B-3+F-1 C-4+E-2+D-6	A1		Either order
	C - 4 + E - 2 + D - 6	A1		Either order
	or			
	first			
	A-4+E-2+D-6	(A1)		
	then }			Must be in this order
	C-4+A-5+B-3+F-1	(A1)		
	or			
	first			
	A-5+B-6	(A1)		
	then	(211)		Must be in this order
		(4.1)		iviust de ili ulis diuei
	C-4+E-2+D-6+B-3+F-1	(A1)		
	M . 1 . 45 . P2 . C4 . P. C . P2 . P3	D.1	_	
	Match A5, B3, C4, D6, E2, F1	B1	5	Must be stated (not solely on diagram)
	Total		7	

MD01 (cont				
Q	Solution	Marks	Total	Comments
2(a)	7	B1		A correct pivot (7 or 22)
	22	B1	2	2 <sup>nd</sup> correct pivot and no others
(b)	<i>C</i>			
	1st 7	B1		
	2nd 5	B1		Condone 7, 5, 3 or $7 + 5 + 3 (= 15)$
	3rd 3	B1	3	unlabelled but must be in this order
(c)	No – 16, 19 haven't been compared (OE)	E1	1	BOTH "No" (or equiv) AND "16, 19"
				(only) mentioned or highlighted in script
	Total		6	
3(a)(i)	EB  (5)	M1		Prim's, MST, 6+ edges (no cycles), edges
	<sub>EH</sub>   7			not lengths or vertices, with first 2 edges
				correct
	$AB \mid 8 \mid$			
	<i>HI</i>	B1		8 edges
	$AD \mid 10$			(Date of
	$\mid DG \mid 4 \mid$	A1		AB 3rd
		A 1	4	A 11
	<i>EF</i>   12	A1	4	All correct
	FC (6)			
(ii)	61	B1	1	
(iii)	$\begin{array}{c c} A & B & C \\ \hline \end{array}$			
		M1		6+ edges, connected, no cycles
	D $E$ $F$			
			_	
	$\bigcap_{G} \bigcap_{H} \bigcap_{I}$	A1	2	Correct, including labelling
	, i			
	D-1-4- D4 DF1 (-1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.	) / 1		DI form their discussion ("")
(b)		M1		PI from their diagram in (iii)
	or			
	a spanning tree with 7 edges not including			
	B (either as a list or diagram)			
	(61 - 13 + 11) = 59	A1	2	Note: 59 scores 2/2
	(01 - 13 + 11) - 39 <b>Total</b>	ΑI	9	1 NOIC. 37 SCUICS 2/2
	1 Otal		7	

MD01 (cont				
Q	Solution	Marks	Total	Comments
4(a)(i)	B 9 3 G 12	M1		(2 values at E or F)
	9 4.5 3	A1		Correct values at E and F
	A 7.5 C 6 H 6 J 3 13.5 24	m1		2 values at <i>I</i>
	0 (13.5) (2t 19.5) (18) (18)	m1		3 values at $J$
	10.5 F13:512 /3	B1		18 at <i>J</i>
	7.5 7.8 [15]	A1	6	All correct, condone 0 missing at A, with rejected values crossed and final values boxed and no extra values at other vertices
(ii)	ADFIJ	B1	1	or reverse
(b)	7.5+ $x$ <12 OE 16.5+ $x$ $\geqslant$ 18 OE	M1		Either correct condone $7 \cdot 5 + x \le 12$ or $16 \cdot 5 + x > 18$
	10.5+x \$18	A1		Both correct
	$1.5 \leqslant x < 4.5$	A1	3	$1.5 \leqslant x < 4.5$ seen (with or without working) scores $3/3$ Condone $1.5 \leqslant x$ and $x < 4.5$ or exact equiv in words but must see "and"
				$1.5 < x$ or $1.5 \leqslant x$ or $x < 4.5$ or $x \leqslant 4.5$
				with no working M1A0
	Total		10	
5(a)	A vertex / vertices of odd order (A, B, G, H) OE	E1	1	Condone statement of non-Eulerian graph
(b)	AB + GH = (180 + 165) = 345 AG + BH = (90 + 210) = 300	M1		These 3 correct sets of pairs
	AH + BG = (150 + 210) = 360	A2,1		3 correct totals, 2 correct totals
	Dist 1215 + 300 PI = 1515	M1 A1	5	1215 + their smallest CSO
(c)(i)	3	B1	1	
(ii)	2	B1	1	
(11)	Total		8	

MD01 (cont		,		,
Q	Solution	Marks	Total	Comments
6(a)(i)	10	B1	1	
(**)	4	D1	1	
(ii)	4	B1	1	
(iii)	5	B1	1	
(111)	3	Di	1	
(b)	eg			
		M1		Simple graph, 6 vertices
		A1	2	Eulerian graph with 9 edges
		AI	2	Eulerian graph with 9 edges
	Total		<b>5</b>	
7(a)	33	B1	1	
(b)	BAEDCB	M1		Tour that visits all vertices
(0)	BAEDCB	A1		Correct tour
	= 41	B1	3	Correct tour
(c)	$A \qquad (3) \qquad B$			Spanning tree without C
				(either drawn or edges listed)
	(4)	M1		and
	(10)	IVII		2 different edges from <i>C</i>
	E			1 1
	A			(either drawn or edges listed)
		A1		Correct MST
	D			
	(11)			
	(5)	A1		Correct 2 edges from C
				Contest 2 suges nom c
	C - 22	D1	4	
	= 33	B1	4	
(d)	A B			
	D			
	E	M1		Correct network
				Possibly earned in (c)
	$\bigvee_{C}$			
	Optimal OE	A1	2	
	Total	111	10	
	1 Otal	I .	10	1

MD01 (cont	()					
Q			Marks	Total	Comments	
8(a)						
	X	A	B			
	0					Condone omission of $X = 0$ , $A = 20$ , $B = 8$
		20	8			
		10				
			16	M1		SCA Trace as far as their '10' at A and
		5				their '16' at B, ignore values in X column
			32	A1		All correct up to and including 32 at B
	32					
		2				
			64	A1		All correct up to and including 64 at <i>B</i>
		1				
			128			
	160			A1	4	All correct and no further working
	("160")					
<i>a</i> >	361010		0.5	D.1		
(b)	Multiplication	l	OE	B1	1	
			OF	F1		
(c)	Continuous lo		OE	E1	2	
	as never reach	Line 90	OE	E1	2	
			Total		7	

MD01 (cont)				
Q	Solution	Marks	Total	Comments
9(a)	$6x + 9y + 9z \le 600$	M1		Any of the three inequalities correct (un)simplified, condone strict inequalities
	$2x + 3y + 3z \le 200$	A1		CAO
	$9x + 6y + 9z \le 600$			
	$3x + 2y + 3z \le 200$	A1		CAO
	$6x + 12y + 18z \ge 480$			
	$x + 2y + 3z \ge 80$	A1	4	CAO
(b)(i)	(z=y)			
	$2x + 3y + 3y \le 200$ or $2x + 6y \le 200$	M1		Correctly substitute into <b>this</b> inequality - either simplified or unsimplified form
	$x + 3y \le 100$ AG			orange simplified of unomprined form
	$3x + 2y + 3z \le 200$			Correctly substitute into <b>this</b> inequality - either simplified or unsimplified form
	$(\Rightarrow) 3x + 5y \le 200$ AG			cluser simplified of unsimplified form
	$x + 2y + 3z \ge 80$			Correctly substitute into <b>this</b> inequality - either simplified or unsimplified form
	$(\Rightarrow) x + 5y \ge 80$ AG	A1	2	All correct – must link their original inequality to the stated answers
(ii)	Each line must be straight to have the B m For all lines, must be correct to ½ square h			al at the indicated vertices.
	y 50	B1		Line through (10, 30) and (40, 20)
	30	B1		Line through (50, 10) and (0, 40)
	20 FR	B1		Line through (80, 0) and (0, 16)
	10 0 20 40 60 80 100 120 x	B1	4	FR, must have all lines correct and labelled region (condone no shading)
(iii)	Max x + 2y   PI	M1		If no statement (PI), then check OL on
	Max (= 25 + 50) = 75	A1	2	diagram, which must be correct for M1 Note: 75 with no working 2/2
(iv)	25 basic, 25 standard, 25 luxury	B1F	1	Condone "25 of each type" ONLY if (b)(iii) fully correct Note $x = 25 = y = z$ B0
	Total	1	13	11000 W 20 y 2 D0
	TOTAL		75	
	IUIAL		13	